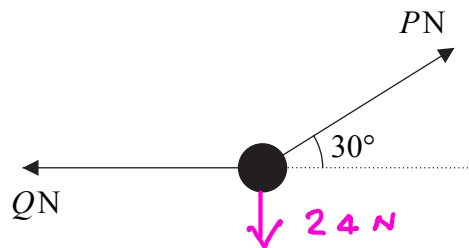


1.

Figure 1



A particle of weight 24 N is held in equilibrium by two light inextensible strings. One string is horizontal. The other string is inclined at an angle of 30° to the horizontal, as shown in Figure 1. The tension in the horizontal string is Q newtons and the tension in the other string is P newtons. Find

(a) the value of P ,

(3)

(b) the value of Q .

(3)

a)



$$P \sin 30^\circ = 24$$

$$\frac{1}{2} P = 24$$

$$P = 48 \text{ N}$$

b)



$$Q = P \cos 30^\circ$$

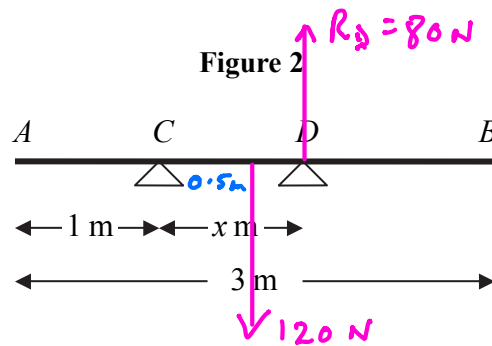
$$Q = 48 \times \frac{\sqrt{3}}{2}$$

$$Q = 24\sqrt{3}$$

$$Q = 41.6 \text{ N}$$



2.



A uniform plank AB has weight 120 N and length 3 m . The plank rests horizontally in equilibrium on two smooth supports C and D , where $AC = 1\text{ m}$ and $CD = x\text{ m}$, as shown in Figure 2. The reaction of the support on the plank at D has magnitude 80 N . Modelling the plank as a rod,

(a) show that $x = 0.75$

(3)

A rock is now placed at B and the plank is on the point of tilting about D . Modelling the rock as a particle, find

(b) the weight of the rock,

(4)

(c) the magnitude of the reaction of the support on the plank at D .

(2)

(d) State how you have used the model of the rock as a particle.

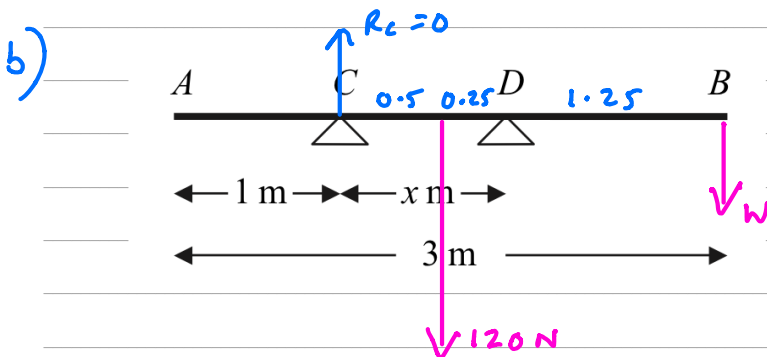
(1)

a) Moments about C

$$120 \times 0.5 = 80x$$

$$\frac{60}{80} = x$$

$$x = 0.75\text{ m}$$



On point of tilting about D, $R_C = 0$



Question 2 continued *Moments about D*

$$W \times 1.25 = 120 \times 0.25$$

$$\text{Rock has weight } W = \frac{30}{1.25} = 24 \text{ N}$$

c) \updownarrow $R_D = 120 + 24 = 144 \text{ N}$

d) *Its weight acts exactly at D*

(Total 10 marks)

Q2



3. A particle P of mass 2 kg is moving under the action of a constant force \mathbf{F} newtons. When $t=0$, P has velocity $(3\mathbf{i} + 2\mathbf{j})\text{ m s}^{-1}$ and at time $t=4\text{ s}$, P has velocity $(15\mathbf{i} - 4\mathbf{j})\text{ m s}^{-1}$. Find

(a) the acceleration of P in terms of \mathbf{i} and \mathbf{j} ,

(2)

(b) the magnitude of \mathbf{F} ,

(4)

(c) the velocity of P at time $t=6\text{ s}$.

(3)

a)

$$\underline{a} = \frac{\underline{v} - \underline{u}}{t} = \frac{\begin{pmatrix} 15 \\ -4 \end{pmatrix} - \begin{pmatrix} 3 \\ 2 \end{pmatrix}}{4} = \frac{\begin{pmatrix} 12 \\ -6 \end{pmatrix}}{4}$$

$$\underline{a} = 3\mathbf{i} - 1.5\mathbf{j} \text{ m s}^{-2}$$

b)

$$\underline{F} = m \underline{a} = 2 \begin{pmatrix} 3 \\ -1.5 \end{pmatrix} = \begin{pmatrix} 6 \\ -3 \end{pmatrix}$$

$$|\underline{F}| = \sqrt{6^2 + (-3)^2} = 6.71 \text{ N}$$

c)

$$\underline{v} = \underline{u} + \underline{a} t$$

$$\underline{v} = \begin{pmatrix} 3 \\ 2 \end{pmatrix} + \begin{pmatrix} 3 \\ -1.5 \end{pmatrix} \times 6$$

$$\underline{v} = \begin{pmatrix} 21 \\ -7 \end{pmatrix} \text{ m s}^{-1}$$

$$\underline{v} = 21\mathbf{i} - 7\mathbf{j} \text{ m s}^{-1}$$



- (a) the value of u ,

(4)

- (2)

(c) Find the value of R .

(4)

5. A ball is projected vertically upwards with speed 21 m s^{-1} from a point A , which is 1.5 m above the ground. After projection, the ball moves freely under gravity until it reaches the ground. Modelling the ball as a particle, find

(a) the greatest height above A reached by the ball,

(3)

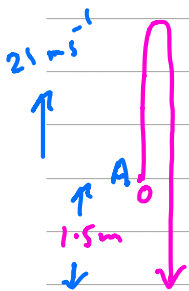
(b) the speed of the ball as it reaches the ground,

(3)

(c) the time between the instant when the ball is projected from A and the instant when the ball reaches the ground.

(4)

a)



$$v^2 = u^2 + 2as$$

At greatest height $v = 0$

$$0^2 = 21^2 - 19.6s$$

$$19.6s = 441$$

$$s = \frac{441}{19.6} = 22.5 \text{ m}$$

Greatest height above $A \approx 22.5 \text{ m}$

b)

$$v^2 = u^2 + 2as$$

$$v^2 = 21^2 - 19.6(-1.5)$$

$$v^2 = 441 + 29.4$$

$$v = -21.7 \text{ m s}^{-1}$$

Speed = 21.7 m s^{-1}



Question 5 continued

c)

$$s = ut + \frac{1}{2}at^2$$

$$-1.5 = 21t - 4.9t^2$$

$$4.9t^2 - 21t - 1.5 = 0$$

$$\text{By calc } t = 4.36s \text{ or } t = -0.070s$$

$$\underline{t = 4.36s}$$

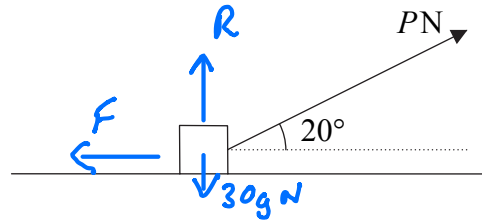
(Total 10 marks)

Q5



6.

Figure 3



A box of mass 30 kg is being pulled along rough horizontal ground at a constant speed using a rope. The rope makes an angle of 20° with the ground, as shown in Figure 3. The coefficient of friction between the box and the ground is 0.4. The box is modelled as a particle and the rope as a light, inextensible string. The tension in the rope is P newtons.

(a) Find the value of P .

(8)

The tension in the rope is now increased to 150 N.

(b) Find the acceleration of the box.

(6)

a)

$$\updownarrow \quad P \sin 20^\circ + R = 30g \quad (1)$$

$$\leftrightarrow \quad P \cos 20^\circ = F$$

$$P \cos 20^\circ = \mu R$$

$$P \cos 20^\circ = 0.4R$$

$$P \cos 20^\circ - 0.4R = 0 \quad (2)$$

Solve (1) and (2) simultaneously by calc

$$P = 109.24 \text{ N}, \quad R = 256.64 \text{ N}$$

$$P = 109 \text{ N}$$

b)

$$\updownarrow \quad 150 \sin 20^\circ + R = 30g$$

$$R = 30g - 150 \sin 20^\circ$$



Question 6 continued

$$\leftrightarrow N2L \quad 150 \cos 20^\circ - F = 30a$$

$$150 \cos 20^\circ - \mu R = 30a$$

$$150 \cos 20^\circ - 0.4(30g - 150 \sin 20^\circ) = 30a$$

$$a = \frac{150 \cos 20^\circ - 0.4(30g - 150 \sin 20^\circ)}{30}$$

$$a = 1.46 \text{ ms}^{-2}$$

Q6

(Total 14 marks)



7.

Figure 4

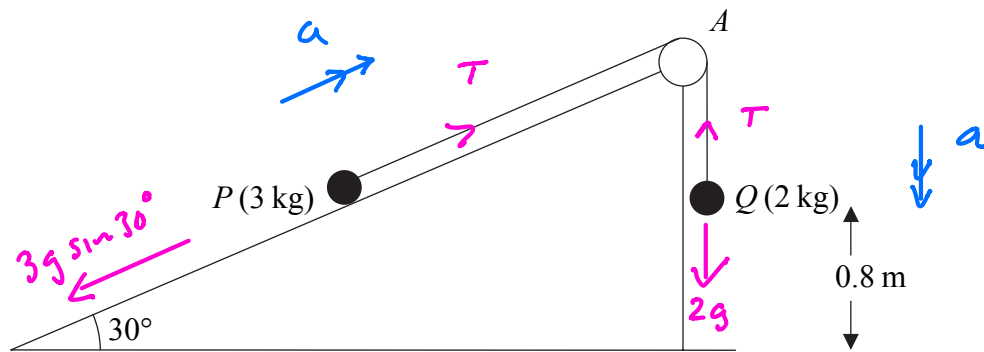


Figure 4 shows two particles P and Q , of mass 3 kg and 2 kg respectively, connected by a light inextensible string. Initially P is held at rest on a fixed smooth plane inclined at 30° to the horizontal. The string passes over a small smooth light pulley A fixed at the top of the plane. The part of the string from P to A is parallel to a line of greatest slope of the plane. The particle Q hangs freely below A . The system is released from rest with the string taut.

(a) Write down an equation of motion for P and an equation of motion for Q . (4)

(b) Hence show that the acceleration of Q is 0.98 m s^{-2} . (2)

(c) Find the tension in the string. (2)

(d) State where in your calculations you have used the information that the string is inextensible. (1)

On release, Q is at a height of 0.8 m above the ground. When Q reaches the ground, it is brought to rest immediately by the impact with the ground and does not rebound. The initial distance of P from A is such that in the subsequent motion P does not reach A . Find

(e) the speed of Q as it reaches the ground, (2)

(f) the time between the instant when Q reaches the ground and the instant when the string becomes taut again. (5)

a) For P $T - 3g \sin 30 = 3a$ ①

For Q $2g - T = 2a$ ②

b) ① + ② $2g - 3g \sin 30 = 5a$



Question 7 continued

$$4.9 = 5a$$

$$\frac{4.9}{5} = a$$

$$a = 0.98 \text{ ms}^{-2}$$

c) $T = 3a + 3g \sin 30^\circ$

$$T = 3 \times 0.98 + 3 \times 9.8 \times 0.5$$

$$T = 17.64$$

$$T = 17.6 \text{ N}$$

d) P and Q have same acceleration

e) $v^2 = u^2 + 2as$

$$v^2 = 0 + 2 \times 0.98 \times 0.8$$

$$v^2 = 1.568$$

$$v = 1.25 \text{ ms}^{-1}$$

f) Starting time when Q hits ground

Parallel to slope NZL for P

(Total 16 marks)

TOTAL FOR PAPER: 75 MARKS

END

Q7



$$-3g \sin 30^\circ = 3a$$

$$-g \sin 30^\circ = a$$

$$a = -4.9 \text{ m s}^{-2}$$

For P parallel to slope $s = ut + \frac{1}{2}at^2$

string becomes taut again when $s = 0$

$$s = 1.25t - \frac{1}{2} \times 4.9t^2$$

$$0 = 1.25t - 2.45t^2$$

$$2.45t^2 - 1.25t = 0$$

$$t(2.45t - 1.25) = 0$$

$$~~t = 0~~ \quad \text{or} \quad t = \frac{1.25}{2.45}$$

$$t = 0.51 \text{ s}$$

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