

Reverse Percentage Problems

- a. In a sale with 25% off a coat is priced at £48.
What was the original price before the sale?

$$\text{Original Price} \times 0.75 = £48$$

$$\text{so } £48 \div 0.75 = \text{Original Price}$$

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- b. After losing 15% of his weight on a diet, a man weighed 68 kg. What was his original weight?

$$\text{Original weight} \times 0.85 = 68 \text{ kg}$$

$$\text{so } 68 \text{ kg} \div 0.85 = \text{original weight}$$

$$68 \text{ kg} \div 0.85 = 80 \text{ kg}$$

- c. A television is priced at £288 inclusive of 20% VAT
What is the price exclusive of VAT?

$$\text{Ex VAT price} \times 1.20 = £288$$

$$\text{so } £288 \div 1.20 = \text{Ex VAT price}$$

$$£288 \div 1.20 = £240$$

- d. After a 5% pay rise John had an hourly rate of pay of £6.72. What was his previous hourly rate of pay?

$$\text{Previous rate} \times 1.05 = £6.72$$

$$\text{so } £6.72 \div 1.05 = \text{Previous rate}$$

$$£6.72 \div 1.05 = £6.40$$

Exercise

11. A workforce is reduced by 5% to 437. What was the previous size of the workforce?
12. Including 20% VAT a television costs £420. What is the ex-VAT price?
13. 442 soldiers completed their training course. If 15% dropped out, how many began the course?
14. A coat is priced at £42 in a sale with 25% off. What was the price of the coat before the sale?
15. After a 15% price rise a cycle cost £184. What was the price before the price rise?

ADVANCED USE OF PERCENTAGES

EXERCISE

10. ~~Decrease £33 by 23%~~
 ~~$100\% - 23\% = 77\%$~~
~~Find 77% of £33~~
 ~~$£33 \times 0.77 = £25.41$~~

14. Original - 25% = £42
 Original $\times 0.75 = £42$
 so $£42 \div 0.75 = \text{original}$
 $£42 \div 0.75 = £56$
 Coat was originally £56

11. Workforce reduced by 5% to 437
 Original $\times 0.95 = 437$
 so $437 \div 0.95 = \text{original}$
 $437 \div 0.95 = 460$
 Original workforce = 460

15. Original + 15% = £184
 Original $\times 1.15 = £184$
 so $£184 \div 1.15 = £160$
 Cycle was originally £160

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12. Ex-VAT price + 20% = £420
 Ex-VAT price $\times 1.20 = £420$
 so $£420 \div 1.20 = \text{Ex-VAT Price}$
 $£420 \div 1.20 = £350$
 Ex-VAT price = £350

13. Original - 15% = 442
 Original $\times 0.85 = 442$
 so $442 \div 0.85 = \text{original}$
 $442 \div 0.85 = 520$
 520 soldiers started course

Reverse Percentages Without a calculator

Ex A TV is £240 including VAT at 20%
 Find ex-VAT

$$\begin{array}{rcl} & £240 & = 120\% \text{ of original} \\ \frac{£240}{6} & £40 & = 20\% \\ £40 \times 5 & £200 & = 100\% \end{array}$$

A coat in a sale with 25% off costs £48. What was pre-sale price

$$\begin{array}{rcl} & £48 & = 75\% \\ £48 \div 3 & £16 & = 25\% \\ £16 \times 4 & £64 & = 100\% \end{array}$$

Exam Question

Adam buys a computer

20% VAT is added to price

Adam pays £900

Work out price before VAT was added

$$\begin{array}{rcl} & £900 & = 120\% \\ \frac{900}{6} & £150 & = 20\% \\ £150 \times 5 & £750 & = 100\% \end{array}$$
