8(i) At P, $x \cos 3x = 0$ $\Rightarrow \cos 3x = 0$ $\Rightarrow 3x = \pi/2, 3\pi/2$ $\Rightarrow x = \pi/6, \pi/2$ So P is $(\pi/6, 0)$ and Q is $(\pi/2, 0)$	M1 M1 A1 A1 [4]	or verification $3x = \pi/2$, $(3\pi/2)$ dep both Ms condone degrees here
(ii) $\frac{dy}{dx} = -3x \sin 3x + \cos 3x$ At P, $\frac{dy}{dx} = -\frac{\pi}{2} \sin \frac{\pi}{2} + \cos \frac{\pi}{2} = -\frac{\pi}{2}$ At TPs $\frac{dy}{dx} = -3x \sin 3x + \cos 3x = 0$ $\Rightarrow \cos 3x = 3x \sin 3x$ $\Rightarrow 1 = 3x \sin 3x / \cos 3x = 3x \tan 3x$ $\Rightarrow x \tan 3x = 1/3 *$	M1 B1 A1 M1 A1cao M1	Product rule $d/dx (\cos 3x) = -3 \sin 3x$ cao (so for $dy/dx = -3x\sin 3x$ allow B1) mark final answer substituting their $-\pi/6$ (must be rads) $-\pi/2$ $dy/dx = 0$ and $\sin 3x / \cos 3x = \tan 3x$ used
(iii) $A = \int_0^{\pi/6} x \cos 3x dx$ Parts with $u = x$, $dv/dx = \cos 3x$ $du/dx = 1$, $v = 1/3 \sin 3x$	B1 M1	Correct integral and limits (soi) – ft their P, but must be in radians
$\Rightarrow A = \left[\frac{1}{3}x\sin 3x\right]_0^{\frac{\pi}{6}} - \int_0^{\pi/6} \frac{1}{3}\sin 3x dx$	A1	can be without limits
$\begin{bmatrix} 1 & 1 & \frac{\pi}{6} \end{bmatrix}$	A1	dep previous A1.
$= \left[\frac{1}{3}x\sin 3x + \frac{1}{9}\cos 3x\right]_{0}^{\frac{\pi}{6}}$	M1dep	substituting correct limits, dep 1 st M1: ft their P provided in radians
$=\frac{\pi}{18}-\frac{1}{9}$	A1 cao [6]	o.e. but must be exact

9(i) ⇒	$f'(x) = \frac{(x^2 + 1)4x - (2x^2 - 1)2x}{(x^2 + 1)^2}$ $= \frac{4x^3 + 4x - 4x^3 + 2x}{(x^2 + 1)^2} = \frac{6x}{(x^2 + 1)^2} *$ When $x > 0$, $6x > 0$ and $(x^2 + 1)^2 > 0$ $f'(x) > 0$	M1 A1 E1 M1 E1	Quotient or product rule correct expression www attempt to show or solve $f'(x) > 0$ numerator > 0 and denominator > 0 or, if solving, $6x > 0 \Rightarrow x > 0$
(ii)	$f(2) = \frac{8-1}{4+1} = 1\frac{2}{5}$ Range is $-1 \le y \le 1\frac{2}{5}$	B1 B1 [2]	must be \leq , y or $f(x)$
\Rightarrow \Rightarrow	f'(x) max when f''(x) = 0 6 - 18 x ² = 0 x ² = 1/3, x = 1/\sqrt{3} f'(x) = $\frac{6/\sqrt{3}}{(1\frac{1}{3})^2} = \frac{6}{\sqrt{3}} \cdot \frac{9}{16} = \frac{9\sqrt{3}}{8} = 1.95$	M1 A1 M1 A1 [4]	$(\pm)1/\sqrt{3}$ oe (0.577 or better) substituting $1/\sqrt{3}$ into $f'(x)$ $9\sqrt{3}/8$ o.e. or 1.95 or better (1.948557)
(iv)	Domain is $-1 < x < 1\frac{2}{5}$ Range is $0 \le y \le 2$	B1 B1 M1 A1 cao	ft their 1.4 but not $x \ge -1$ or $0 \le g(x) \le 2$ (not f) Reasonable reflection in $y = x$ from $(-1, 0)$ to $(1.4, 2)$, through $(0, \sqrt{2}/2)$ allow omission of one of -1 , 1.4 , 2 , $\sqrt{2}/2$
	$y = \frac{2x^2 - 1}{x^2 + 1} x \leftrightarrow y$ $x = \frac{2y^2 - 1}{y^2 + 1}$ $xy^2 + x = 2y^2 - 1$ $x + 1 = 2y^2 - xy^2 = y^2(2 - x)$ $y^2 = \frac{x + 1}{2 - x}$ $y = \sqrt{\frac{x + 1}{2 - x}} *$	M1 M1 M1	(could start from g) Attempt to invert clearing fractions collecting terms in y^2 and factorising www