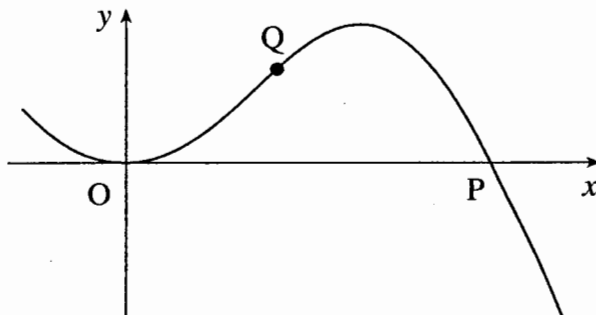


**Section B (36 marks)**

- 8 Fig. 8 shows part of the curve  $y = x \sin 3x$ . It crosses the  $x$ -axis at P. The point on the curve with  $x$ -coordinate  $\frac{1}{6}\pi$  is Q.



**Fig. 8**

- (i) Find the  $x$ -coordinate of P. [3]
- (ii) Show that Q lies on the line  $y = x$ . [1]
- (iii) Differentiate  $x \sin 3x$ . Hence prove that the line  $y = x$  touches the curve at Q. [6]
- (iv) Show that the area of the region bounded by the curve and the line  $y = x$  is  $\frac{1}{72}(\pi^2 - 8)$ . [7]

- 9 The function  $f(x) = \ln(1 + x^2)$  has domain  $-3 \leq x \leq 3$ .

Fig. 9 shows the graph of  $y = f(x)$ .

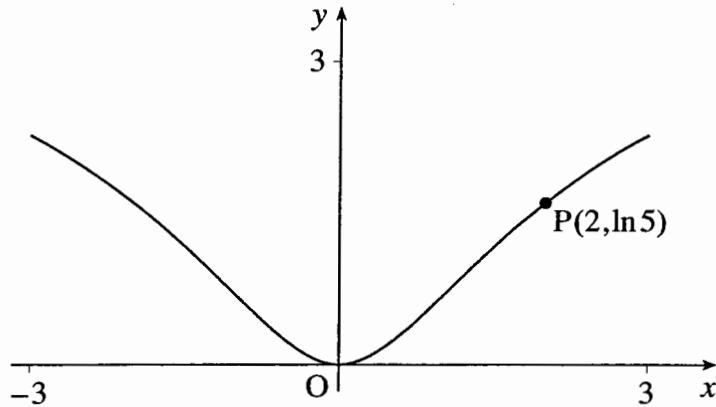


Fig. 9

- (i) Show algebraically that the function is even. State how this property relates to the shape of the curve. [3]
- (ii) Find the gradient of the curve at the point  $P(2, \ln 5)$ . [4]
- (iii) Explain why the function does not have an inverse for the domain  $-3 \leq x \leq 3$ . [1]

The domain of  $f(x)$  is now restricted to  $0 \leq x \leq 3$ . The inverse of  $f(x)$  is the function  $g(x)$ .

- (iv) Sketch the curves  $y = f(x)$  and  $y = g(x)$  on the same axes.

State the domain of the function  $g(x)$ .

Show that  $g(x) = \sqrt{e^x - 1}$ . [6]

- (v) Differentiate  $g(x)$ . Hence verify that  $g'(\ln 5) = 1\frac{1}{4}$ . Explain the connection between this result and your answer to part (ii). [5]