

| Topics | What students need to learn: |  |  |
| :---: | :---: | :---: | :---: |
|  | Content |  | Guidance |
| 4 Sequences and series continued | 4.2 | Work with sequences including those given by a formula for the $n$th term and those generated by a simple relation of the form $x_{n+1}=\mathrm{f}\left(x_{n}\right) ;$ <br> increasing sequences; decreasing sequences; periodic sequences. | For example $u_{n}=\frac{1}{3 n+1}$ describes a decreasing sequence as $u_{n+1}<u_{n}$ for all integer $n$ <br> $u_{n}=2^{n}$ is an increasing sequence as $u_{n+1}>u_{n}$ for all integer $n$ $u_{n+1}=\frac{1}{u_{n}}$ for $n>1$ and $u_{1}=3$ describes a periodic sequence of order 2 |
|  | 4.3 | Understand and use sigma notation for sums of series. | Knowledge that $\sum_{1}^{n} 1=n$ is expected |
|  | 4.4 | Understand and work with arithmetic sequences and series, including the formulae for $n$th term and the sum to $n$ terms | The proof of the sum formula for an arithmetic sequence should be known including the formula for the sum of the first $n$ natural numbers. |
|  | 4.5 | Understand and work with geometric sequences and series, including the formulae for the $n$th term and the sum of a finite geometric series; the sum to infinity of a convergent geometric series, including the use of $\|r\|<1$; modulus notation | The proof of the sum formula should be known. <br> Given the sum of a series students should be able to use logs to find the value of $n$. <br> The sum to infinity may be expressed as $S_{\infty}$ |
|  | 4.6 | Use sequences and series in modelling. | Examples could include amounts paid into saving schemes, increasing by the same amount (arithmetic) or by the same percentage (geometric) or could include other series defined by a formula or a relation. |

