

## Paper 1 and Paper 2: Pure Mathematics

To support the co-teaching of this qualification with the AS Mathematics qualification, common content has been highlighted in bold.

Topics	What students need to learn:		
	Content	Guidance	
<b>1</b> <b>Proof</b>	1.1	<p><b>Understand and use the structure of mathematical proof, proceeding from given assumptions through a series of logical steps to a conclusion; use methods of proof, including:</b></p> <p><b>Proof by deduction</b></p> <p><b>Proof by exhaustion</b></p> <p><b>Disproof by counter example</b></p> <p>Proof by contradiction (including proof of the irrationality of <math>\sqrt{2}</math> and the infinity of primes, and application to unfamiliar proofs).</p>	<p><b>Examples of proofs:</b></p> <p><b>Proof by deduction</b></p> <p><b>e.g. using completion of the square, prove that <math>n^2 - 6n + 10</math> is positive for all values of <math>n</math> or, for example, differentiation from first principles for small positive integer powers of <math>x</math> or proving results for arithmetic and geometric series. This is the most commonly used method of proof throughout this specification</b></p> <p><b>Proof by exhaustion</b></p> <p><b>This involves trying all the options. Suppose <math>x</math> and <math>y</math> are odd integers less than 7. Prove that their sum is divisible by 2.</b></p> <p><b>Disproof by counter example</b></p> <p><b>e.g. show that the statement "<math>n^2 - n + 1</math> is a prime number for all values of <math>n</math>" is untrue</b></p>