## Vertical SUVAT



## J une 2011 <br> Mechanics M1 6677

## Mark Scheme



| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5 (a) | $\begin{aligned} v=u+a t(\uparrow) \Rightarrow 0 & =u-g\left(\frac{25}{14}\right) \\ u & =171 / 2 * \end{aligned}$ | $\begin{gathered} \text { M1 M(A) } 1 \\ \text { A1 } \end{gathered}$ |
| (b) | $\begin{aligned} v^{2}=u^{2}+2 a s(\uparrow) \Rightarrow>0^{2} & =17.5^{2}-2 g s \\ s & =15.6 \quad(\mathrm{~m}) \quad \text { or } 16(\mathrm{~m}) \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |
|  |  | (2) |
| (c) | $s=u t+\frac{1}{2} a t^{2}(\uparrow)=>6.6=17.5 t-\frac{1}{2} g t^{2}$ | M1 |
|  | $4.9 t^{2}-17.5 t+6.6=0$ | A1 |
|  | $t=\frac{17.5 \pm \sqrt{ }\left(17.5^{2}-129.36\right)}{9.8}=\frac{17.5 \pm 13.3}{9.8}$ | DM1 |
|  | $\begin{array}{llll} t= & 9.8 & 9.8 \\ t & =3.142 \ldots(22 / 7) & \text { or } & 0.428 \ldots(3 / 7) \end{array}$ | A1 |
|  | $\begin{equation*} T=t_{2}-t_{1}=2.71 \tag{2.7} \end{equation*}$ | DM1 A1 (6) |
|  | OR $\begin{gathered} v^{2}=u^{2}+2 a s(\uparrow) \Rightarrow>v^{2}=17.5^{2}-2 g \times 6.6 \\ v= \pm 13.3 \end{gathered}$ |  |
|  | $v=u+a t(\uparrow)=> \pm 13.3=17.5-g t$ | M1A1 |
|  | $17.5 \pm 13.3$ | DM1 |
|  | $\begin{aligned} & =\frac{9.8}{} \\ & =3.14 . .(22 / 7) \text { or } 0.428 . .(3 / 7) \end{aligned}$ | A1 |
|  | $T=3.14 . .-0.428 . .=2.71 \text { or } 2.7$ | DM1 A1 (6) |
|  | OR |  |
|  | $\begin{aligned} v^{2}=u^{2}+2 a s(\uparrow) \Rightarrow v^{2}=17.5^{2}-2 g \times 6.6 & \text { or } & 0^{2}=u^{2}-2 g \mathrm{x}(15.625-6.6) \\ v=13.3 & & u=13.3 \end{aligned}$ |  |
|  | $v=u+a t(\uparrow) \Rightarrow 0=13.3-g t$ | M1 A1 |
|  | $t=\frac{13.3}{o}$ | DM1 A1 |
|  | $T=2 \times \frac{13.3}{\sigma}=2.7 \text { or } 2.71$ | DM1 A1 (6) |


| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 5. | $v^{2}=u^{2}+2 a s \Rightarrow 28^{2}=u^{2}+2 \times 9.8 \times 17.5$ <br> Leading to $u=21$ | cso | $\begin{array}{\|l} \text { M1 A1 } \\ \text { A1 } \tag{3} \end{array}$ |
|  | (b) $\begin{aligned} & s=u t+\frac{1}{2} a t^{2} \Rightarrow 19=21 t-4.9 t^{2} \\ & 4.9 t^{2}-21 t+19=0 \\ & t=\frac{21 \pm \sqrt{21^{2}-4 \times 4.9 \times \mathrm{x} 19}}{9.8} \end{aligned}$ |  | M1 A1 |
|  | $\begin{aligned} & t=2.99 \text { or } 3.0 \\ & t=1.30 \text { or } 1.3 \end{aligned}$ |  | DM1 A1 A1 <br> (5) |
|  | (c) $\begin{array}{ll} \mathrm{N} 2 \mathrm{~L} \quad & 4 g-5000=4 a \\ & (a=-1240.2) \\ v^{2}=u^{2}+2 a s \Rightarrow 0^{2}=28^{2}-2 \times 1240.2 \times s \end{array}$ |  | M1 A1 |
|  | Leading to $s=0.316(\mathrm{~m})$ | or 0.32 | $\begin{array}{\|lr} \text { M1 A1 } & \text { (4) } \\ & {[\mathbf{1 2}]} \end{array}$ |
|  | OR $\frac{1}{2} \times 4 \times 28^{2}+4 g s=5000 s$ <br> Work-Energy: $s=0.316 \text { or } 0.32$ |  | M1 A1 M1 A1 |

## Question 5(a)

First M1 for a complete method for finding $u$ e.g.

$$
28^{2}=u^{2}+2 g \times 17.5
$$

or $28^{2}=u^{2}+2(-g) \times(-17.5)$
or $28^{2}=2 g s \Rightarrow s=40$ then $0^{2}=u^{2}+2(-g) \times(22.5)$
condone sign errors
First A1 for a correct equation(s) with $g=9.8$
Second A1 for " $u=21$ " PRINTED ANSWER
N.B. Allow a verification method, but they must state, as a conclusion, that " $u=21$ ", to score the final A1.

## Question 5(b)

First M1 for a complete method for finding at least one $t$ value i.e. for producing an equation in $t$ only. (condone sign errors but not missing terms)
First A1 for a correct quadratic equation in $t$ only or TWO correct linear equations in $t$ only.
Second DM1, dependent on first M1, for attempt to solve the quadratic or one of the linear equations.
Second A1 for 3.0 or 3 or 2.99
Third A1 for 1.3 or 1.30

## Question 5(c)

First M1 for resolving vertically with usual rules.
First A1 for a correct equation
Second M1 for use of $v^{2}=u^{2}+2 a s$, with $v=0, u=28$ or $u=0$ and $v=28$ and their $a$, (or any other complete method which produces an equation in $s$, which could be negative)
M0 if they haven't calculated a value of $a$.
Second A1 for 0.32 or 0.316 . (must be positive since it's a distance)


