

7. The lines l_1 and l_2 have equations

$$\mathbf{r} = \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 3 \\ 4 \end{pmatrix} \quad \text{and} \quad \mathbf{r} = \begin{pmatrix} \alpha \\ -4 \\ 0 \end{pmatrix} + \mu \begin{pmatrix} 0 \\ 3 \\ 2 \end{pmatrix}.$$

If the lines l_1 and l_2 intersect, find

- (a) the value of α , (4)
- (b) an equation for the plane containing the lines l_1 and l_2 , giving your answer in the form $ax + by + cz + d = 0$, where a , b , c and d are constants. (4)

For other values of α , the lines l_1 and l_2 do not intersect and are skew lines.

Given that $\alpha = 2$,

- (c) find the shortest distance between the lines l_1 and l_2 .
- (3)**



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Question 7 continued

Handwriting practice area with horizontal lines.





Question 7 continued

- 6.** The plane P has equation

$$\mathbf{r} = \begin{pmatrix} 3 \\ 1 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 0 \\ 2 \\ -1 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ 2 \\ 2 \end{pmatrix}$$

- (a) Find a vector perpendicular to the plane P . (2)

The line l passes through the point $A(1, 3, 3)$ and meets P at $(3, 1, 2)$.

The acute angle between the plane P and the line l is α .

- (b) Find α to the nearest degree. (4)

- (c) Find the perpendicular distance from A to the plane P . (4)

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Question 6 continued

Lined area for writing the answer to Question 6.



(a) $\overrightarrow{AC} \times \overrightarrow{BC}$,

This is a vector product and not on Core Pure syllabus

(b) the area of triangle ABC ,

(2)

(c) an equation of the plane ABC in the form $\mathbf{r} \cdot \mathbf{n} = p$

(2)

