

Integration

Differentiation

$$\frac{d}{dx} ax^n = nax^{n-1}$$

$$\frac{d}{dx} \ln ax = \frac{1}{x}$$

$$\frac{d}{dx} \ln(f(x)) = \frac{f'(x)}{f(x)}$$

$$\frac{d}{dx} ae^x = ae^x$$

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\frac{d}{dx} \sin ax = a \cos ax$$

$$\frac{d}{dx} \cos ax = -a \sin ax$$

Integration

$$\int ax^n dx = \frac{ax^{n+1}}{n+1} + C$$

$$\int \frac{1}{x} dx = \ln|x| + C$$

$$\int \frac{f'(x)}{f(x)} dx = \ln(f(x)) + C$$

$$\int ae^x dx = ae^x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\int \cos ax dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax + C$$

Exercise 11 A

$$\text{d) } \int \left(3\sec^2 x + \frac{5}{x} + \frac{2}{x^2} \right) dx = \int \left(3\sec^2 x + \frac{5}{x} + 2x^{-2} \right) dx$$
$$= 3\tan x + 5\ln|x| - \frac{2}{x} + C$$

$$\text{c) } \int 2(\sin x - \cos x + x) dx$$
$$= 2\left(-\cos x - \sin x + \frac{x^2}{2}\right) + C$$

$$\text{e) } \int \left(5e^x + 4\cos x - \frac{2}{x^2} \right) dx$$
$$= \int \left(5e^x + 4\cos x - 2x^{-2} \right) dx$$
$$= 5e^x + 4\sin x + 2x^{-1} + C$$

$$\text{g) } \int \left(\frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} \right) dx$$
$$= \int \left(\frac{1}{x} + x^{-2} + x^{-3} \right) dx$$
$$= \ln|x| + \frac{x^{-1}}{-1} + \frac{x^{-2}}{-2} + C$$
$$= \ln|x| - \frac{1}{x} - \frac{1}{2x^2} + C$$

$$1b) \int (5e^x - 4\sin x + 2x^3) dx$$

$$= 5e^x + 4\cos x + \frac{x^4}{2} + C$$

$$1d) \int (3\sec x \tan x - \frac{2}{x}) dx$$

$$= 3\sec x - 2\ln|x| + C$$

$$1f) \int \left(\frac{1}{2x} + 2\csc^2 x \right) dx$$

$$= \frac{1}{2}\ln|x| - 2\cot x + C$$

$$1h) \int (e^x + \sin x + \cos x) dx$$

$$= e^x - \cos x + \sin x + C$$

$$1j) \int (e^x + \frac{1}{x} - \csc^2 x) dx$$

$$= e^x + \ln|x| + \cot x + C$$

Hulc - Video lesson on Integration by Substitution
Print lesson notes, do exercise and self-mark