

# Inequalities

Ex 1

$$2x + 3 = 11$$

$$2x = 11 - 3$$

$$2x = 8$$

$$x = \frac{8}{2}$$

$$x = 4$$

$$2x + 3 < 11$$

$$2x < 11 - 3$$

$$2x < 8$$

$$x < \frac{8}{2}$$

$$x < 4$$

Ex 2

$$8x - 7 = 5x + 11$$

$$8x - 5x = 11 + 7$$

$$3x = 18$$

$$x = \frac{18}{3}$$

$$x = 6$$

$$8x - 7 \geq 5x + 11$$

$$8x - 5x \geq 11 + 7$$

$$3x \geq 18$$

$$x \geq \frac{18}{3}$$

$$x \geq 6$$

Ex 3

$$4x + 1 = 7x + 16$$

$$4x - 7x = +16 - 1$$

$$-3x = 15$$

$$x = \frac{15}{-3}$$

$$4x + 1 \leq 7x + 16$$

$$4x - 7x \leq 16 - 1$$

$$-3x \leq 15$$

$$x \geq \frac{15}{-3}$$

$$x = -5$$

$$x \geq -5$$

Alternative Solution

$$4x + 1 = 7x + 16$$

$$+1 - 16 = 7x - 4x$$

$$-15 = 3x$$

$$\frac{-15}{3} = x$$

$$-5 = x$$

$$\underline{x = -5}$$

$$4x + 1 \leq 7x + 16$$

$$+1 - 16 \leq 7x - 4x$$

$$-15 \leq 3x$$

$$\frac{-15}{3} \leq x$$

$$-5 \leq x$$

$$\underline{x \geq -5}$$

Exercise 3D Page 47

$$\begin{aligned} 1b) \quad 5x + 4 &\geq 39 \\ 5x &\geq 39 - 4 \\ 5x &\geq 35 \\ x &\geq \frac{35}{5} \\ \underline{x &\geq 7} \end{aligned}$$

$$\begin{aligned} 1d) \quad 5x + 6 &\leq -12 - x \\ 5x + x &\leq -12 - 6 \\ 6x &\leq -18 \\ x &\leq \frac{-18}{6} \\ \underline{x &\leq -3} \end{aligned}$$

$$\begin{aligned} 1f) \quad 21 - 2x &> 8 + 3x \\ -2x - 3x &> 8 - 21 \\ -5x &> -13 \\ x &< \frac{-13}{-5} \\ x &< 2.6 \end{aligned}$$

$$\begin{aligned} 1j) \quad 5x + 4 &> 12 - 2x \\ 5x + 2x &> 12 - 4 \\ 7x &> 8 \end{aligned}$$

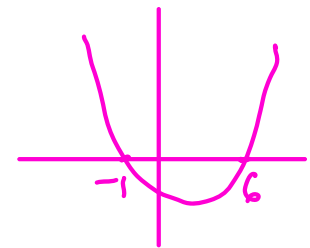
$$\begin{aligned}
 1h) \quad 7x - 7 &< 7 - 7x \\
 7x + 7x &< 7 + 7 \\
 14x &< 14 \\
 x &< \frac{14}{14} \\
 x &< 1
 \end{aligned}$$

$$x > \frac{8}{7}$$

## Quadratic Inequalities

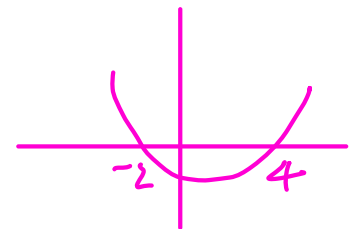
$$\begin{aligned}
 \text{Ex1} \quad x^2 - 5x - 6 &< 0 \\
 (x+1)(x-6) &< 0 \\
 -1 &< x < 6
 \end{aligned}$$

$$y = x^2 - 5x - 6$$



$$\begin{aligned}
 \text{Ex2} \quad x^2 - 2x - 8 &\geq 0 \\
 (x+2)(x-4) &\geq 0
 \end{aligned}$$

$$y = x^2 - 2x - 8$$

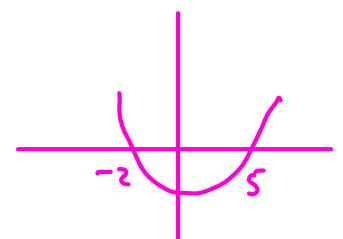


$$\begin{aligned}
 \text{Either } x &\geq 4 \\
 \text{or } x &\leq -2
 \end{aligned}$$

## Exercise 3E

$$\begin{aligned}
 1c) \quad x^2 - 3x - 10 &> 0 \\
 (x+2)(x-5) &> 0
 \end{aligned}$$

$$y = x^2 - 3x - 10$$



$$\begin{aligned}
 \text{Either } x &> 5 \\
 \text{or } x &< -2
 \end{aligned}$$

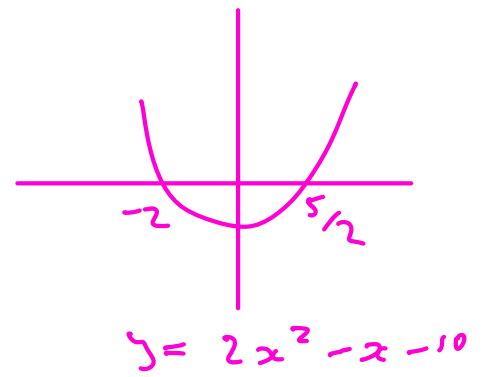
$$1f) \quad 10 + x - 2x^2 < 0$$

$$0 < 2x^2 - x - 10$$

$$0 < (2x - 5)(x + 2)$$

$$\text{Entweder } x > \frac{5}{2}$$

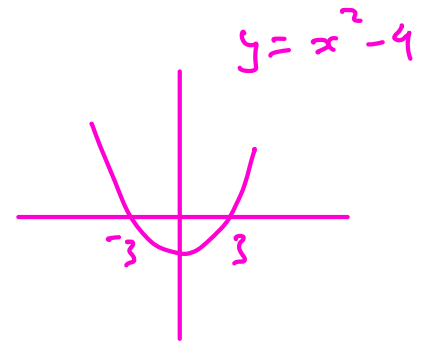
$$\text{or } x < -2$$



$$1i) \quad x^2 - 9 < 0$$

$$(x + 3)(x - 3) < 0$$

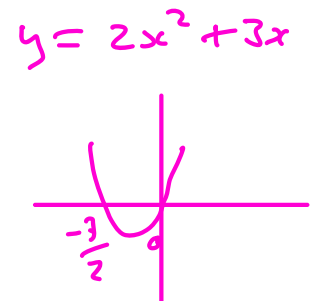
$$-3 < x < 3$$



$$1e) \quad 2x^2 + 3x \leq 0$$

$$x(2x + 3) \leq 0$$

$$-\frac{3}{2} \leq x \leq 0$$



Homework (for Tuesday)

Exercise 3D Q2 c, f, i, e

Exercise 3E Q1 a, d, g, j

Q2 b, d