

## Proof

It is suggested that to square an integer and a half you multiply the integer by the next integer and add  $\frac{1}{4}$ .

$$\begin{aligned}\text{Proof } \left(n + \frac{1}{2}\right)^2 &= n^2 + \frac{1}{2}n + \frac{1}{2}n + \frac{1}{4} \\ &= n^2 + n + \frac{1}{4} \\ &= n(n+1) + \frac{1}{4}\end{aligned}$$



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## Identities

$$(n+1)^2 \equiv n^2 + 2n + 1$$

True for all values of  $n$

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## Proof Exercise 7E

1) Proof by exhaustion

$$1 \leq n \leq 6$$

$m = n+2$  is not divisible by 10

$n=1$	$m=3$	} not divisible by 10
$n=2$	$m=4$	
$n=3$	$m=5$	
$n=4$	$m=6$	
$n=5$	$m=7$	
$n=6$	$m=8$	

5) a)  $n^4 - n$  is divisible by 4

Counter example  $n=2$

$$2^4 - 2 = 14 \text{ not divisible by 4}$$

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b) Perfect squares have an odd number of factors  
eg 9 has 1, 3, 9

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c)  $2n^2 - 6n + 1 > 0$  for all  $n$

$$n=1 \quad 2(1)^2 - 6(1) + 1 = -3 \quad \times$$

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d)  $2n^2 - 2n - 4$  is multiple of 3

$$n=3 \quad 2(3)^2 - 2(3) - 4 = 8$$

not a multiple of 3  $\times$

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