

Bounds Problems

Ex 1

A carpet measures 3.60 m by 2.40 m
each measurement correct to nearest 10 cm
Find upper and lower bounds for its area
and perimeter.

$$\text{Area} = L \times W \quad \text{Perimeter} = 2L + 2W$$

$$3.55 \leq L < 3.65$$

$$2.35 \leq W < 2.45$$

$$\begin{aligned} \text{Upper Bound For Area} &= \max L \times \max W \\ &= 3.65 \times 2.45 \\ &= \underline{8.9425 \text{ m}^2} \end{aligned}$$

$$\begin{aligned} \text{Lower Bound for Area} &= \min L \times \min W \\ &= \underline{8.3425 \text{ m}^2} \end{aligned}$$

$$\begin{aligned} \text{Upper Bound for Perimeter} \\ &= 2 \times 3.65 + 2 \times 2.45 = 12.2 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Lower Bound for Perimeter} \\ &= 2 \times 3.55 + 2 \times 2.35 = 11.8 \text{ m} \end{aligned}$$

Ex 2

John runs 100 m in 12 seconds
The distance is measured to the nearest 5 m

and the time is measured to the nearest second
Find upper and lower bounds for his average speed

$$97.5 \leq \text{Distance} < 102.5$$

$$11.5 \leq \text{Time} < 12.5$$

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$

$$\begin{aligned} \text{Upper Bound for Speed} &= \frac{\text{Max Distance}}{\text{Min Time}} = \frac{102.5}{11.5} \\ &= \underline{8.91 \text{ m s}^{-1}} \end{aligned}$$

$$\begin{aligned} \text{Lower Bound for Speed} &= \frac{\text{Min Distance}}{\text{Max Time}} = \frac{97.5}{12.5} \\ &= \underline{7.8 \text{ m s}^{-1}} \end{aligned}$$

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1a) Area $5\text{ cm} \times 9\text{ cm}$ (nearest cm)

$$8.5 \leq \text{Length} < 9.5$$

$$4.5 \leq \text{width} < 5.5$$

$$8.5 \times 4.5 \leq \text{Area} < 9.5 \times 5.5$$

$$38.25\text{ cm}^2 \leq \text{Area} < 52.25\text{ cm}^2$$

Hwk Revise For Indices test on Monday